

lengths
of

A

W. 7. 2

$$\frac{dP(t')}{d\Omega} =$$

$$\frac{dt}{dt'} = 1 + \frac{d}{c dt'} R(t')$$

recall $R = |\vec{x} - \vec{r}(t')|$

$$\frac{dt}{dt'} = (1 - \vec{\beta} \cdot \hat{n})$$

so $\frac{dP(t')}{d\Omega} = \frac{e^2}{4\pi c}$



Since most of radiation is in the forward direction, eff carries over to total energy as well as angular distribution

linear motion

$$\vec{\beta} \parallel \dot{\vec{\beta}}$$

$$\vec{\beta} \cdot \hat{n} \equiv \beta \cos \theta$$

θ angle between
+ direction

we've seen this in
NR se

$$\frac{dP(t')}{d\Omega} = \frac{e^2 \beta}{4\pi c} \frac{\sin^2 \theta}{(1 - \beta \cos \theta)^5} \frac{dP}{d\phi d\cos \theta}$$

for $\cos \theta_{\max}$ or u_{\max}

$$\text{i.e. } -\frac{2u}{(1-\beta u)^5} = 0$$

$$\text{or } \frac{1}{(1-\beta u)^6} \{ 2u(-\beta u) + 5(1-u^2)\beta \} = 0$$

$$3\beta u^2 + 2u - 5\beta = 0$$

$$u_{\max} = \frac{1}{3\beta} \left(-1 + (1 + 5\beta^2)^{1/2} \right)$$

$$\beta \rightarrow 0 \quad u_{\max} \rightarrow 0 \quad \theta_{\max} \approx \pi/2$$

$\beta \rightarrow$ write

$$1 + 1 + 1$$

$$= \frac{1}{3} \left(1 + \frac{1}{2\gamma^2} \right) \left(-1 + 4 \left(1 - \frac{5}{32\gamma^2} \right) \right)$$

$$= \left(1 + \frac{1}{2\gamma^2} \right) \left(1 - \frac{5}{8\gamma} \right) = 1 - \frac{1}{8\gamma^2} = \cos \theta_{\max}$$

$$= -\frac{\theta_{\max}^2}{2}$$

\Rightarrow

γ^2

$$\frac{dp}{d\alpha}$$

$\gamma \rightarrow$

$$\pi^0 \rightarrow \gamma + \gamma$$

\rightarrow
 θ
 \rightarrow

$$E_\pi = 2E_\gamma$$

$$P_\pi = 2p_\gamma \cos\theta$$

$$\frac{c}{E_\pi} = \beta_\pi = \frac{2c \gamma \cos\theta}{E} =$$

$$\beta \approx 1 - \frac{1}{2\gamma^2} = 1 - \frac{\theta^2}{2}$$

$$\Rightarrow \theta \approx \frac{1}{\gamma}$$



again forward peaked (factors of $1 - \cos\theta$)

$\bar{x} \bar{x}$
 z

Path d

ΔL

$$t - t_1$$

$$\frac{P}{2\gamma^3 c}$$



$$\omega_c = \frac{3}{2} \gamma^3 \frac{c}{P}$$

characteristic
frequency
for spec
distribution

$\frac{1}{2}$

$$\frac{dW}{d\Omega} = \int_{-\infty}^{\infty} |\vec{A}(t)| dt$$

$$\vec{A}(t) = \left(\frac{1}{2\pi}\right)^2 \int_{-\infty}^{\infty} \vec{A}(\vec{\omega}) e^{-i\omega t} \omega$$

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Par

$$- \int_{-\infty}^{\infty} |d\omega|$$